An Improved Time-Reversal-Based Target Localization for Through-Wall Microwave Imaging

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ABSTRACT

Recently, time reversal (TR) method, due to its high functionality in heterogeneous media has been widely employed in microwave imaging (MI) applications. One of the applications turning into a great interest is through-wall microwave imaging (TWMI). In this paper, TR method is applied to detect and localize a target obscured by a brick wall using a numerically generated data. Regarding this, it is shown that when the signals acquired by a set of receivers are time reversed and backpropagated to the target-embedded media, finding the optimum time frame which the constituted image represents a true location of the target becomes infeasible. Indeed, there are situations pertinent to the target distance ratio that the previously-used Maximum field method and Entropy-based methods may fail to select the optimum time frame. As a result, an improved method which is based on initial reflection from the target is proposed. According to different target locations described in this research, the results show this method prevails over the shortcomings of the former methods.

1. INTRODUCTION

Recently, in the field of microwave imaging (MI), the great interest on detection and localization of objects through walls and obstacles has been emerging. This phenomenon basically arises from various unique civilian and military applications, including non-destructive detection tests, earthquake search and rescue missions, hostage operations or hostile threat assessment situations [1]. In fact, a through-wall microwave imaging (TWMI) system would be capable of collecting information of the total media consisting of target(s) and wall(s), performing a comprehensive process on it, and also identify and localize the target. Encouraging results have been obtained with backscattering algorithms [2], synthetic-aperture-radar (SAR) [3], polarimetric-based techniques [4], tomographic approach [5], and high-speed imaging algorithm known as Envelope [6].

However, among the processing algorithms, time reversal (TR) methods have shown that would exploit ultra wide band (UWB) signals and the concept of multipath components in the intervening media to ameliorate the detection capabilities [7]. Originally, TR has been utilized in acoustics [8]. Also, it has been introduced in Electromagnetics and more research has been carried out on subsurface object imaging [9], wireless communication systems [10], bio-malignant tissue detection [11, 12], and through-wall imaging of the obscured targets [13-15].

In TR method, a source radiates a signal which propagates through a media including the target. The waves are then reflected and the corresponding data are recorded by an array of receivers. By extracting the target-only responses from the data, reversing them in time and synthetically propagating them back, an image of the scene can be extracted at each time frame. Consequently, by utilizing an appropriate approach to take an optimum time frame, detection
and localization of the target becomes possible. Furthermore, in TWMI applications, TR entails to detect targets through materials including plywood, drywall, solid/hollow brick and concrete which their relative high permittivity or inhomogeneous structure may result in further burden for selecting the optimum time frame.

In this paper, we embark on solving the problem of finding an optimum time frame which represents an exact image of the target. In this regard, *Maximum Electric-field (E-field) Method* [13] and *Entropy-based Methods* [11, 14] have been recently employed in both TWMI and breast cancer detection scenarios. These methods may guarantee a maximum amplitude or a tightly focused image corresponding to the detected location of the target. However, we show that there are situations pertinent to the distance ratio of the target in which the preceding methods may fail to image the exact location of the target. As a result, an improved method, based on *initial reflection from the target* is proposed which is robust to the effect of this parameter and prevails over the previous methods.

The rest of the paper is organized as follows: in Section II a general description of TR method is presented. In Section III, the geometry of TWMI scenarios along with the specifications of computational setup is introduced which is carried out numerically using finite-difference time-domain (FDTD) [16]. In Section IV, the methods of finding an optimum time frame together with our proposed method are fully addressed. The results regarding the functionality of the methods to successfully localize the target according to different distance ratios of the target are demonstrated in Sections V. Finally, in Section VI a summary of the present work and the future contributions is drawn.

2. CLASSIC TR METHOD

Time Reversal (TR) technique is an imaging method based on the invariance of Maxwell’s equations under time reversal, which is known in electromagnetics as the principle of reciprocity. In general, the procedure for detection and localization of the target based on TR consists of three main steps shown in Fig. 1.

After, a source radiates a signal through a media including the targets, the reflected waves from the media are recorded by an array of receiving antennas which ideally should be placed all around the media to capture all the possible directions of the reflected waves. However, unlike this full-aspect configuration [17], in other types of scenarios, it is presumably impossible to entirely surround the media and a limited number of arrays are particularly feasible.

Then, the reflected waves from the media are recorded by an array of receiving antennas which ideally should be placed all around the media to capture all the possible directions of the reflected waves. However, unlike this full-aspect configuration [17], in other types of scenarios, it is presumably impossible to entirely surround the media and a limited number of arrays are particularly feasible. This limited-aspect configuration is in prevalent use for the applications including TWMI and subsurface objects imaging. Thereupon, the aim of forward propagation step is to collect the data of the media and process them in order to image and localize the targets. Accordingly, the data can be generated either analytically [7], numerically [11-13], or physically via on-site measurement [14], in which the first two suffice when one deals with the development of imaging algorithms such that spending time and energy on practical measurements is almost cumbersome.

Next, the target-only response must be extracted from the recorded signal at each array receiver. Since the recorded signal of the media consists of background clutter plus target, assuming that the background is stationary, its solo signature with no target in present can be calculated and collected at each receiver. Now, let’s assign $E_T$ and $E_B$ as the total and background reflected signals, respectively. Then, for each receiver, the target-only (scattered) response $E_S$ is obtained as

$$E_S = E_T - E_B$$

(1)

This method of extracting the target response is called background subtraction method. In fact, extracting the target response is the basis of all TR processing methods including Classic TR [11], DORT [9, 18], MUSIC [19] and TRAIC [20]. In scenarios in which $E_B$ cannot be obtained in a separate run, the target response is directly extracted from the total response by applying a time-window on the total signal [9] or Matched-Filter analysis [21]. However, these methods...
will surely yield to more mathematical efforts. Additionally, in moving target scenarios, the information about $E_0$ may not be required and corresponding target response can be achieved using the total response subtraction of two successive moving target runs. This method is called differential TR and is fully addressed in [22].

In the final step, based on TR processing method used in the previous step, imaging and localization of the target become possible. By time-reversing (phase conjugating in frequency domain) the target responses at each array receiver and synthetically propagating them back to the background media (no target), the wave focuses on the location of formerly existing target, approximating recreating the image of the target. It is obvious that this step is performed analytically by using Green functions named Point Spread Functions (PSF) [23] or numerically including FDTD [11-13], TLM [24], and Ray-Tracing methods [25]. Despite this, unlike the imaging applications, physical back propagation of the waves may occur in applications involving actual retransmission of signals like destruction of kidney stones with ultrasonic waves [26].

3. GEOMETRY AND COMPUTATIONAL SETUP

A. Geometry of TWMI Problem

The geometry of TWMI problem which is considered in this investigation is depicted in Fig 2. A standard commercial solid brick cell with dimensions 20×10 cm (length × width) is used here to construct a single layer wall with 10 cm thickness and 120 cm vertical length. Based on the measurement results reported in [27], the relative permittivity and conductivity of the brick wall is nearly consistent in the entire frequency spectrum of the measurement. As a result, regarding to the center frequency of excitation source, these values are set to $\varepsilon_r=4.8$ and $\sigma=0.001$ S/m.

A linear array of 16 isolated z-directed electric dipoles with equidistant separation of 6 cm are placed just 20 cm before the wall to act as the receiving probes. These arrays are called time reversal array (TRA) and will participate in synthetically back propagation step. The distance between the first and the last probe is called aperture size $a$ which is equal to 90 cm for this array. A z-directed electric dipole at the center of the array line is placed as the transmitter (and as monostatic receiver) to radiate the excitation pulse toward the scene in $TM_z$ mode. Also, throughout this work, a cylindrical disk scatterer with diameter $D=6$ cm and $\varepsilon_r=47$ will be introduced as a target in different locations behind the wall, generally specified as near distance and far distance with respect to aperture size $a$. More discussion about this issue will be given in part D.

![Figure 2: FDTD computational setup used for TWMI. The source (dot) and TRA (stars) are shown. The brick wall has 10 cm thickness. The target will be introduced at different locations. The aperture size and target distance are also denoted by $a$ and $L$, respectively.](image)

B. Computational Setup for TR Method

Both forward-propagation and back-propagation steps of TR method are carried out numerically using two-dimensional finite-difference-time-domain (FDTD) method. The computational domain has a dimension of $N_x\times N_y=180\times130$ grid points, with a uniform spatial discretization of $\Delta=1$ cm and a time step of $\Delta t=16$ ps (the Courant factor $S_C=c\Delta t/\Delta x$ is chosen to be 0.5). The maximum of runtime is also set to $\text{maxtime}=800\Delta t$ which is sufficiently enough for the incident wave to travel from the source to the right end of the domain in a round-trip. The boundary condition used is also a convolutional perfectly matched layer (CPML) formulated with recursive-convolution technique to provide reflectionless truncation of the computation domain. The thickness of CPML is set to $5\Delta$ at all four sides of the boundaries.

It is also worth noting that in medium with high losses or dispersion, the performance of TR imaging based on conventional FDTD may become degraded due to double attenuation in forward and back propagation steps. To dispel this problem, a modification on FDTD update equations must be performed at back-propagation step in order to compensate losses or dispersion caused by the background media [11, 28].

C. Excitation Source

In general, various constraints and specifications including particular electrical characteristics of the media, signal penetration through wall materials, target dimensions, and also portability of the setup will determine the best operating frequency range for microwave penetrating radar (MPR) systems. Practically, such systems operate in the range of 0.5-
10 GHz [29] and a minimum system bandwidth of about 30% with respect to the center frequency is essential for providing a sufficient resolution in target detection [4]. In this work, a UWB modulated Gaussian pulse is considered as the excitation source by

\[ P(t) = e^{\left(\frac{t-t_0}{t_p}\right)^2} \sin \left(2\pi f_p(t-t_0)\right) \]  

(2)

Where \( t_0 \) and \( t_s \) are temporal width and temporal shift, respectively, which specify the spectrum bandwidth of \( P(t) \) and also \( f_p \) is the center frequency. These parameters are then assigned as \( f_p=4.6 \) GHz, \( t_p=0.16 \) ns and \( t_s=2*t_p \). The excitation pulse and its frequency spectrum is also plotted in Fig. 3.

D. Final Settings

Assume that the target is located at a distance \( L \) away from the source. We may further investigate TR method according to the distance \( L \) with respect to \( a \); simply \( L/a \) (originated from classical diffraction limit). As a result, there will be three distance ratios as near distance \( L/a<1 \), medium distance \( L/a=1 \), and far distance \( L/a>1 \). Finally, to fully understand the capability of TR method, two general near and far distance settings shown in Table 1 will be specified in this paper.

4. Focusing Methods

After exciting the source and collecting the data of reflected signals, we obtain target-only responses by using background subtraction methods. The target responses are then time reversed and backpropagated into the background media. Accordingly, the computationally backpropagated fields constitute an image of the scene at each frame of the time. Next, we embark on solving a problem of finding an optimum timeframe which represents an image of the scene with exact focusing on the location of the target.

A. Maximum E-field Method

As reported by Zheng et al. [13], in this method the maximum E-field amplitude of the imaging domain is found at each time frame and it is plotted along the time axis. The optimum time frame is then selected as a time which corresponds to the maximum of this plot, as

\[ t_{opt} = \left\{ t': E_{max}(t') > E_{max}(t), t_0 < t < t_1 \text{ & } t \neq t' \right\} \]  

(3)

TABLE 1

<table>
<thead>
<tr>
<th>Setting 1</th>
<th>Setting 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Target Location ((x,y))</td>
<td>(70,40)</td>
</tr>
<tr>
<td>Target Distance Ratio</td>
<td>near</td>
</tr>
</tbody>
</table>

B. Entropy-based Methods

In the ideal full-aspect configuration, the behavior of backpropagated waves on target location is such that it first converges toward the target and a time lag behind that, it diverges from it. In order to find a time frame which is corresponding to the convergence-divergence instant, a minimum entropy criterion will be defined as in (5) and (6) reported by Cresp et al [14] and Kosmas et al [11], respectively.

\[ p_{ij}^n = \frac{\sum E_n^2(i,j)}{\sum_{i,j} E_n^2(i,j)} \]  

(4)

\[
ENT(n) = -\sum_{i,j} p_{ij}^n \ln p_{ij}^n \max(p_{ij}^n)
\]  

(5)

\[
ENT(n) = \left[ \sum_{i,j} E_n^2(i,j) \right]^{-2} \sum_{i,j} E_n^4(i,j)
\]  

(6)

Where \( n \) represents the time frame, \((i,j)\) the grid cell coordinates and the summation is over the entire imaging domain. The defined entropy is calculated at each time frame and a time instant when it becomes minimized is selected as the optimum time frame. Unlike the previous method, minimum entropy method guarantees a tightly focused image rather than maximum field amplitude at the focusing point.
C. Target Initial Reflection Method

In this work, we examine the functionality and efficiency of the above focusing methods and investigate the situations in which they may fail to image the exact location of the target. As a result, an alternative optimum time focusing method which is valid for all situations and prevails over the shortcomings of other methods should be utilized. In this part we are attempting to characterize this proposed method, namely Target Initial Reflection Method.

Let’s again postulate the geometry of the wall and an arbitrary located target as in Fig. 4. Now, we want to follow the transmitted wave starting at the beginning source point, propagating into the scene, possessing interactions with the wall and the target, and then reflecting back to the receiving arrays. In addition, we will monitor the target response waveforms of three particular receivers; the source receiver, which corresponds to a receiver at the source point \( R_S \), the nearest receiver to the target \( R_N \), and the farthest receiver away from the target \( R_F \). The excited source after a delay of \( t_d \) reaches to the peak value. In its path toward the target, it travels the route \( A_1B_1, B_1C_1 \) and \( C_1D \), where \( D \) is the point which the transmitted wavefront is incident on the target. The target scatters the fields and a portion of them are received by the arrays. For the source receiver \( R_S \) the scattered wave travels \( DC_2, C_2B_2 \) and \( B_2A_2 \), likewise the wave travels \( DC_3, C_3B_3 \) and \( B_3A_2 \) to reach to nearest receiver \( R_N \) and \( DC_1, C_2B_1 \) and \( B_1A_1 \) to reach to farthest receiver \( R_F \). The detailed waveforms monitored by each of these three receivers are shown in Fig. 5.

The received waves are then time-reversed and back-propagated, which is analogous to start the propagation from the right end of each waveform (maxtime) and move toward the left (Fig. 5). According to the depicted waveforms, the first antenna starting backpropagation process is the farthest one, it travels along the path toward the target up until the time the nearest antenna as the last antenna starts backpropagation. Based on Fig. 5 it is derived the two waveforms will simultaneously reach the target location \( D \) if they both travel only the remained time amount of \( t_2 \) which is the stacked time for the scattered waveform to travel from the target \( D \) to the nearest receiver at \( A_1 \). As a result, these two waveforms together with the waveform from the rest of the arrays will arrive at the same time to point \( D \) and their amplitudes are constructively added to each other to construct a contrasted image of the location of the target. More detailed route path of backpropagated waveforms are shown in Fig. 4.

In other words, the optimum time frame is a time instant in which the nearest receiver \( R_N \) is powered on and then continues traveling for \( t_2 \) sec. To formulate the optimum time, we may write

\[
 t_{\text{opt}} = \left( \text{maxtime} - (t_d + t_1 + t_2) \right) + t_2
\]

\[= \text{maxtime} - (t_d + t_1) \quad (7)\]

where \( t_1 \) is the stacked time for the source waveform to travel from starting point \( A_1 \) to target \( D \) or vice versa. According to the waveform of the source receiver

\[
t_r = t_d + 2t_1 \quad \Rightarrow \quad t_1 = \frac{t_r - t_d}{2} \quad (8)
\]
Figure 6: Curves of optimum time frame for Maximum E-field Method, Entropy-based Methods Eq. (5) and Eq. (6), and Target Initial Reflection Method. (a) Near distance target (setting 1), (b) Far distance target (setting 2).

Where $t_i$ is the time when the initial reflection from the target arrives to the source receiver. As a result, by knowing the maxtime along with $t_d$ and $t_r$, substituting (8) in (7), the optimum time frame $t_{opt}$ could be readily derived as

$$t_{opt} = \text{maxtime} - \frac{t_r - t_d}{2}$$

The optimum time frame based on target initial reflection method guarantees well that the backpropagated waves of the entire receivers will simultaneously focus on a desired location which represents the target location. Here, further investigations prove that the analysis is independent of excitation sources and the wall parameters.

5. LOCALIZATION OF THE TARGET

In this section, we investigates localization of a target for the settings defined in Section III and apply the focusing methods introduced in Section IV to select the optimum time frame for the target location.

Fig. 6 shows the corresponding curves for each of the focusing methods. Plots (a) and (b) also pertain to near and far distance ratios of the target. The optimum time frame derived by Target Initial Reflection Method is also determined by a vertical dashed line in each setting. All the curves are plotted from 200$\Delta t$ which is an instant the backpropagated waves pass the wall, up to the maximum runtime of 800$\Delta t$. In order to compare the methods, the curves are normalized with respect to their corresponded maximum value. As it can be seen, plots of Maximum E-field Method have a monotonically increasing manner insofar as it reaches to the maximum and then starts to descend. Besides, in the case of multiple targets, additional local maxima are emerged instead of one global maximum.

The Entropy-based Methods are monotonically decreasing up until their minimum value. Also noticeable is the small variation of Entropy-based Method (5) over almost the entire time axis. Furthermore for the cases the target is located at the right end of the imaging domain, as in setting 2 (Fig. 6b), Entropy-based Method (6) will have a global minimum (marked with red dot) which may be misled as the optimum time frame regarding the location of the target, whereas this minimum basically corresponds to the time instances the computationally backpropagated waves are exiting the imaging domain. Therefore the actual valid minimum is the one which is taking place at a time before reaching to this minimum. Finally, the optimum time frame concluded from the above curves for each method is depicted in Table 2. The difference (in terms of $\Delta t$) between each optimum time frame method with respect to Target Initial Reflection Method is also cited in parentheses.

Next, the images of spatial refocusing constituted by each method are demonstrated in Fig. 7 and Fig. 8 regarding near distance and far distance target location, respectively. The focused wave features a white region and the true location of the target is drawn as a small black circle. For near distance target (Fig. 7), it is clear from the images that the accurate focusing is almost achieved for all the methods including Maximum E-field Method, Entropy-based Methods, and Target Initial Reflection Method. On the other hand, when the target is located at far distance (Fig. 8), for all the methods (except Target Initial

<table>
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<th>Table 2</th>
<th>CALCULATED OPTIMUM TIME FRAME FOR EACH METHOD</th>
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</thead>
<tbody>
<tr>
<td>Setting 1</td>
<td>Setting 2</td>
</tr>
<tr>
<td>Max E-field</td>
<td>610 (9)</td>
</tr>
<tr>
<td>Entropy-based, Eq. (5)</td>
<td>614 (5)</td>
</tr>
<tr>
<td>Entropy-based, Eq. (6)</td>
<td>614 (5)</td>
</tr>
<tr>
<td>Target Initial Reflection</td>
<td>619</td>
</tr>
</tbody>
</table>


Figure 7: The images constituted by TR processing for target located at near distance (Setting 1) regarding optimum time frame methods of (a) Maximum E-field Method, (b) Entropy-based Methods Eq. (5), (c) Entropy-based Methods Eq. (6), (d) Target Initial Reflection Method.

Figure 8: The images constituted by TR processing for target located at far distance (Setting 2) regarding optimum time frame methods of (a) Maximum E-field Method, (b) Entropy-based Methods Eq. (5), (c) Entropy-based Methods Eq. (6), (d) Target Initial Reflection Method.
Accurate focusing was almost achieved for all the methods with the accuracy about less than one target size shift. However, for the far distance target, the only method which can estimate the target as much accurate as possible was Target Initial Reflection Method and all the other methods was failed to accurately focus on the target. In general, Target Initial Reflection Method prevailed over other methods without being totally dependent on the target different locations.

Future works may include:
1. Utilizing and evaluating this method in real TWMI scenarios where the nature of experimental environment would cause more deterioration for accurate localization of the target.
2. Applying this method for applications such as biological and under-the-ground imaging which their media are much heterogeneity.

7. REFERENCES


BIographies

Amin B. Gorji was born in Cardiff, UK, in 1989. He received the B.Sc. degree in electrical engineering from Babol Noshirvani University of Technology, Babol, Iran, in 2011, where he is currently advancing his M.Sc. degree in Electromagnetics engineering.

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